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Panalytical**

# Complementary Techniques

Particle size, distribution & charge linking rheology

**Anamet Seminar, 2019**

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Malvern Panalytical, Malvern, WR14 1XZ, UK (previously Malvern Instruments Limited)

(40 mins)

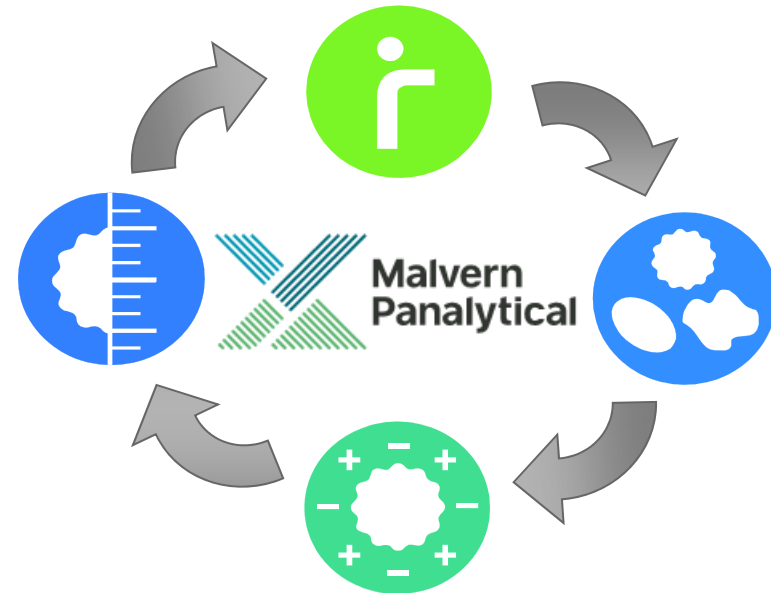
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May 2019

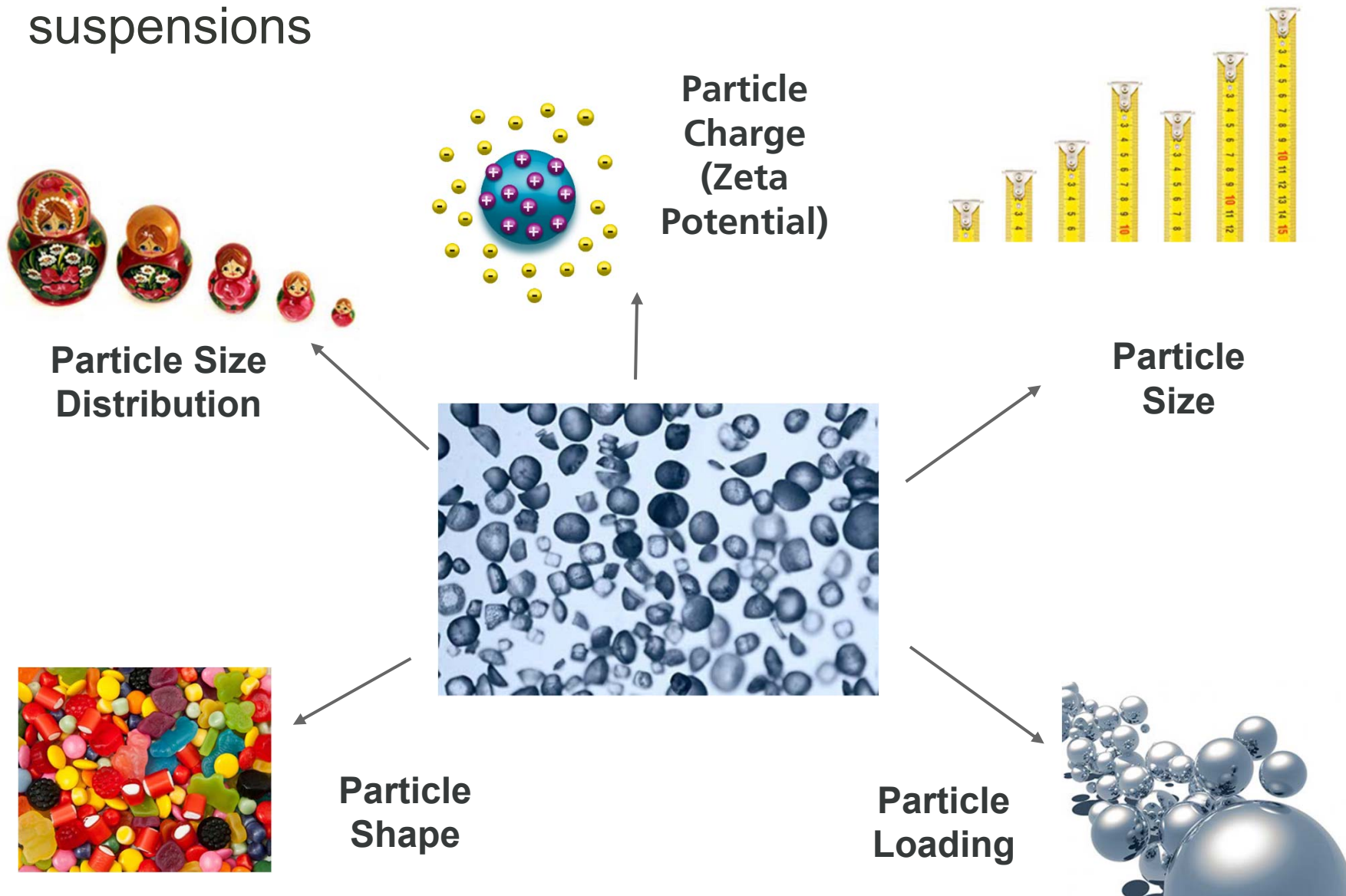
# Overview



- Rheology Overview
- How particle properties link to rheology
- Suspension Stability
  - Particle Size
  - Particle Loading
  - Particle Size Distribution



# Rheology-determining factors of suspensions



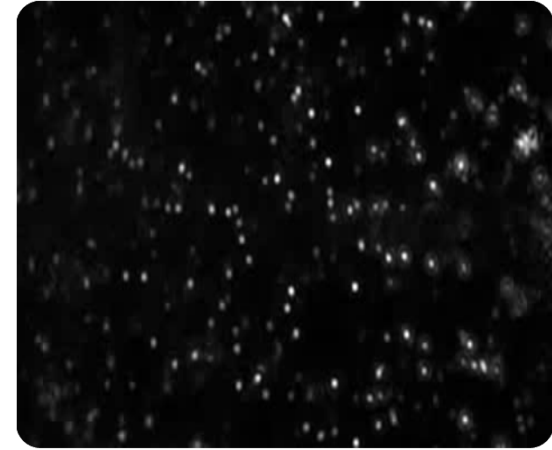
# PARTICLE SIZE



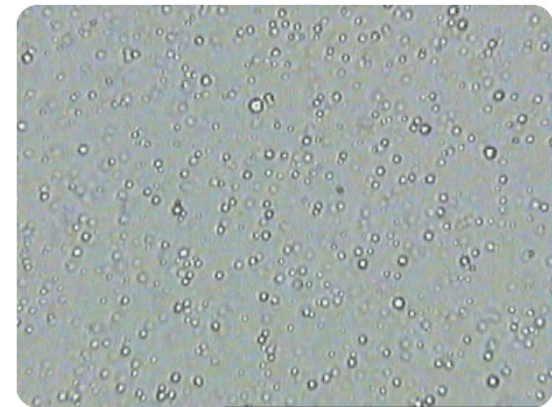
# Effect of particle size

- For **small** ( $< \sim 1 \mu\text{m}$ ) particles colloidal effects on rheological properties can be significant:
  - Brownian motion
    - The random movement of particles due to the bombardment by the solvent molecules that surround them
  - Attractive / repulsive colloidal forces
- For **large** ( $> \sim 1 \mu\text{m}$ ) particles the direct effect on rheology is much less
  - The affect is more related to the associated change in volume fraction

Nanoparticles (**small**)



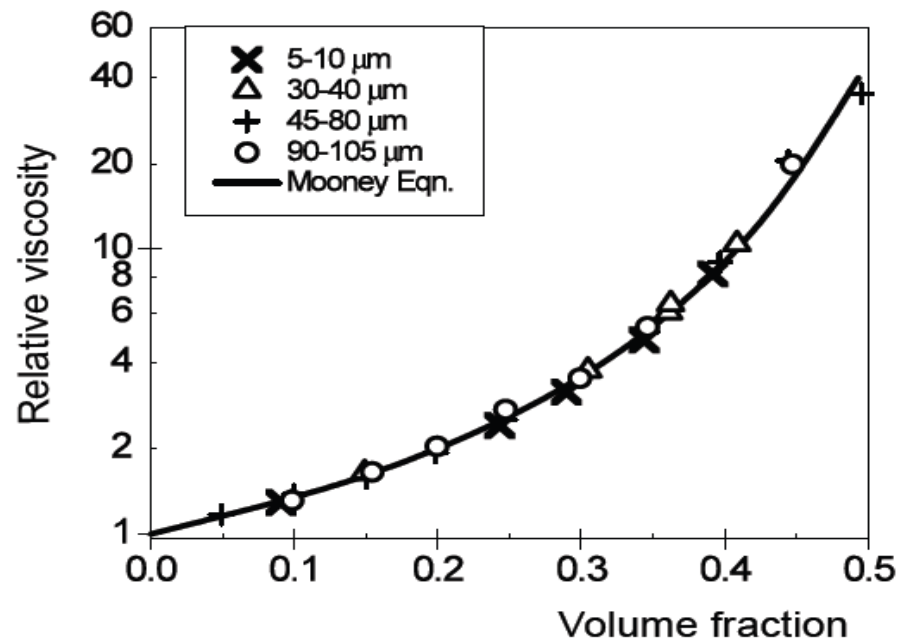
Emulsion Droplets (**large**)



# Effect of particle size

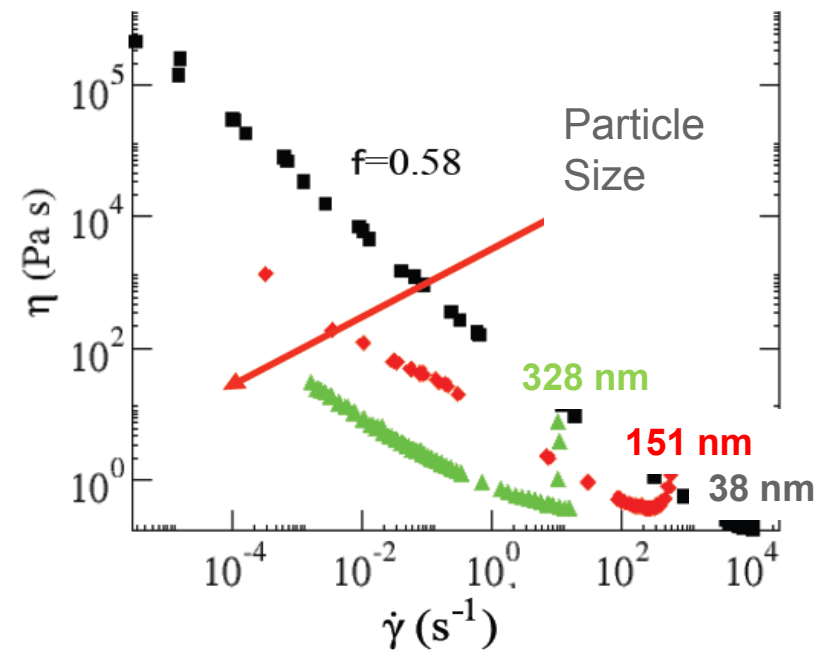
- For **large particles** ( $> \sim 1 \mu\text{m}$ ) the direct effect of increasing size shows **little viscosity difference** for the **same volume fraction**
- **Increasing volume fraction** for the same particle size, increases viscosity
- › For **small particles**, ( $< \sim 1 \mu\text{m}$ ) there is a relationship
- › **Decreasing** particle size gives a **increased** viscosity

## Large particles



*Colloidal Suspension Rheology Jan Mewis, Norman J. Wagner, 2012*

## Small particles



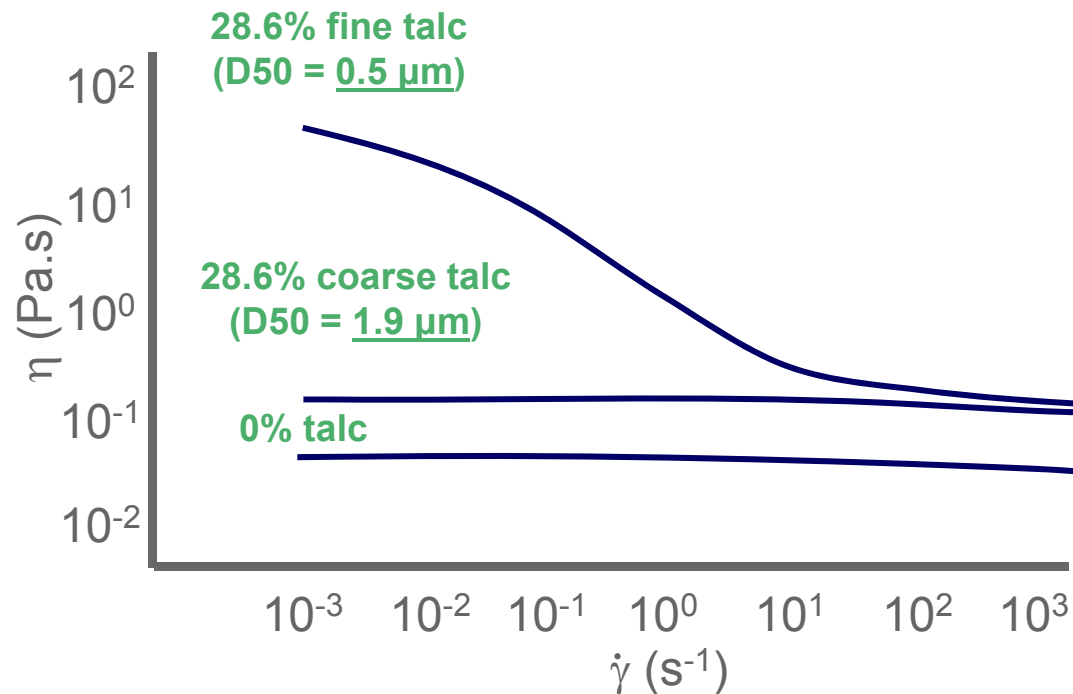
*Lewis & Nielsen 1968*

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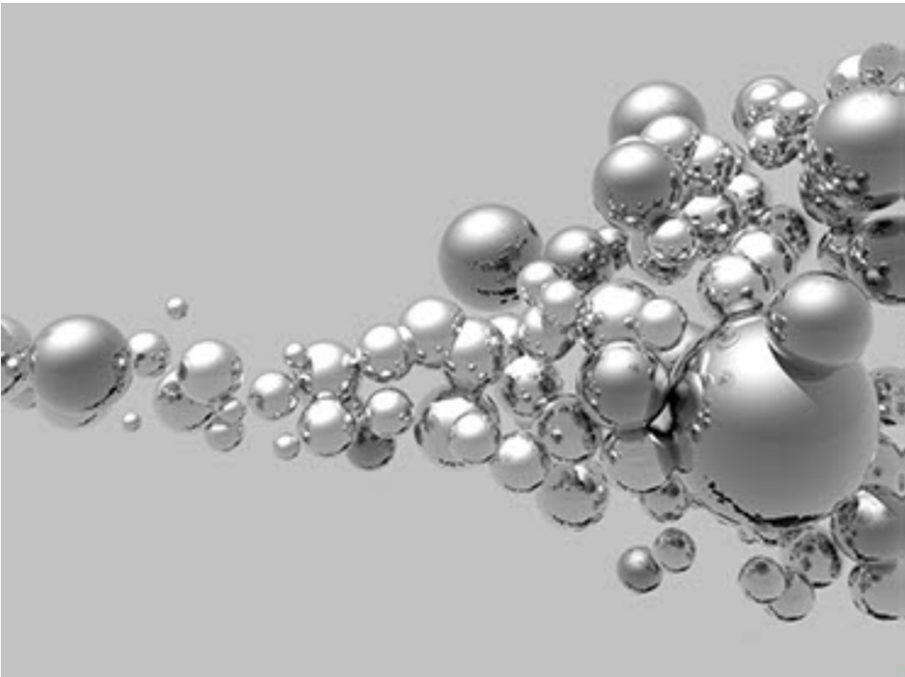
# Effect of particle size

- Adding coarse talc to an epoxy
- For constant volume fraction **decreasing particle size will increase viscosity**
- The increased number of small particles give rise to **colloidal repulsion**, increasing viscosity at **low shear**



➤ This relatively weak force is broken down at higher shear rate leading to the converging of viscosities

# PARTICLE LOADING





# Effect of particle loading

## Krieger-Dougherty equation

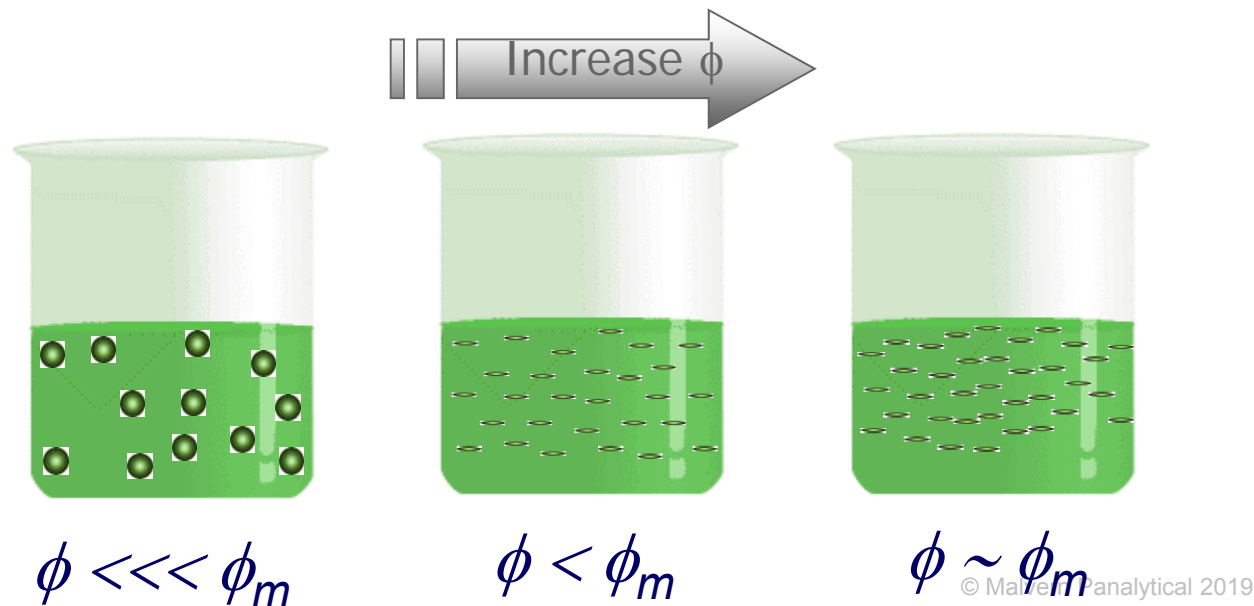
$$\frac{\eta}{\eta_{medium}} = \left( 1 - \frac{\phi}{\phi_m} \right)^{-[\eta]\phi_m}$$



- ▶  $\eta$  – viscosity of the suspension
- ▶  $\eta_{medium}$  – viscosity of the medium
- ▶  $\phi$  – volume fraction of solids in the suspension
- ▶  $\phi_m$  – maximum vol. fraction of solids in the suspension
- ▶  $[\eta]$  – intrinsic viscosity of the medium (2.5 for spheres)

# Volume fraction, $\phi$

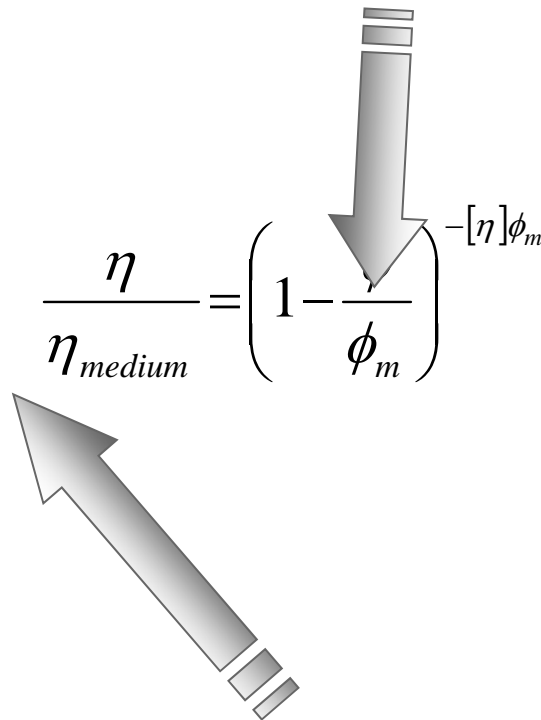
- Describes the **amount of particles** in a material
- $\phi$  – volume fraction of solids in a suspension
- $\phi_m$  – maximum volume fraction of solids in the suspension (i.e. the maximum amount of particles that can be added to the suspension)

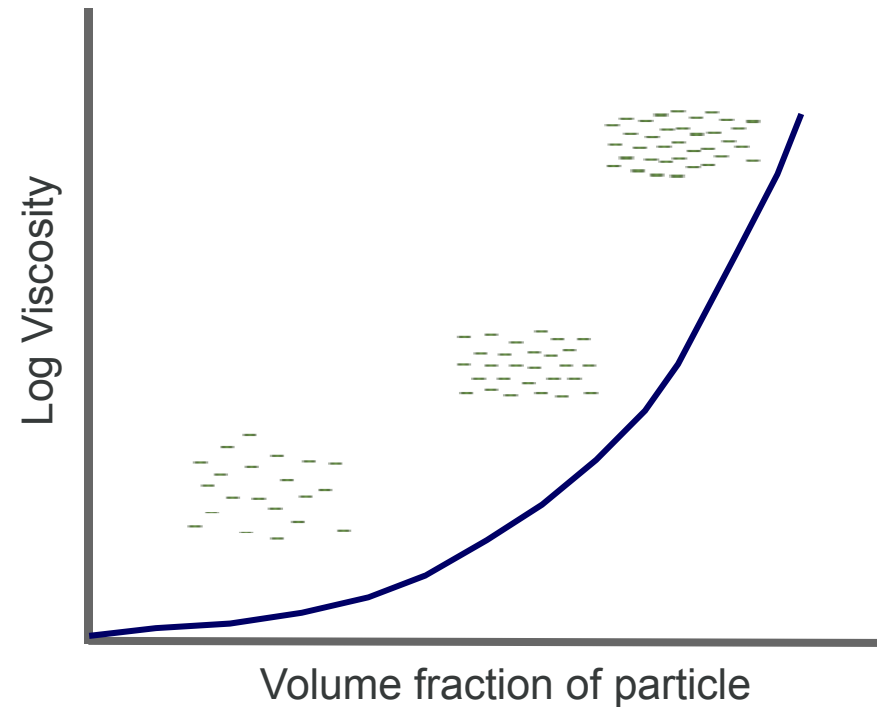


# Effect of particle loading

As volume fraction ( $\phi$ ) increases...



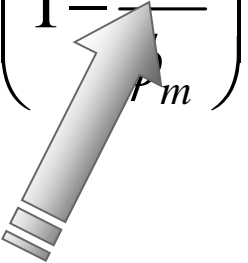
$$\frac{\eta}{\eta_{medium}} = \left(1 - \frac{\phi_m}{\phi_m}\right)^{-[\eta]\phi_m}$$




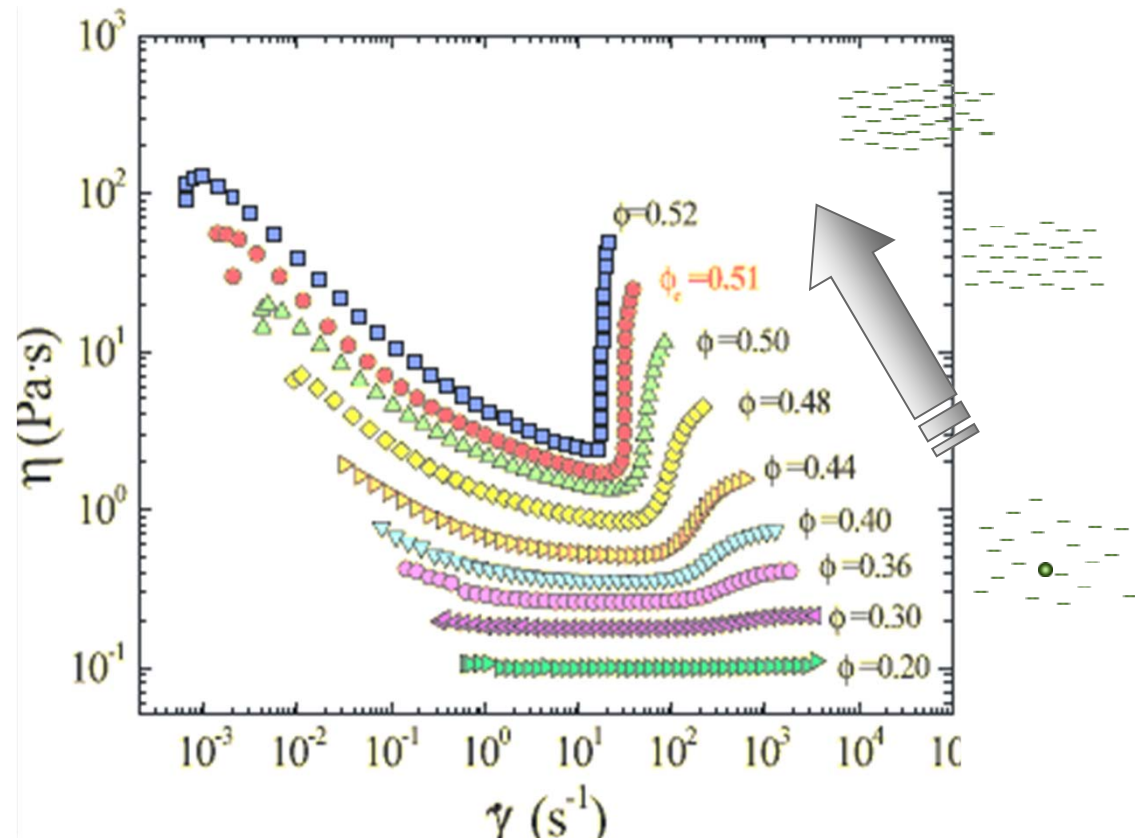
- › Then **viscosity ( $\eta$ ) increases.**
- › Packing more molecules makes flow more difficult.

# Volume fraction

- Viscosity ( $\eta$ ) is increasing with an increased volume fraction as suggested by **Krieger-Dougherty**

$$\frac{\eta}{\eta_{medium}} = \left(1 - \frac{\phi}{\phi_m}\right)^{-[\eta]\phi_m}$$


- Packing more molecules makes flow more difficult



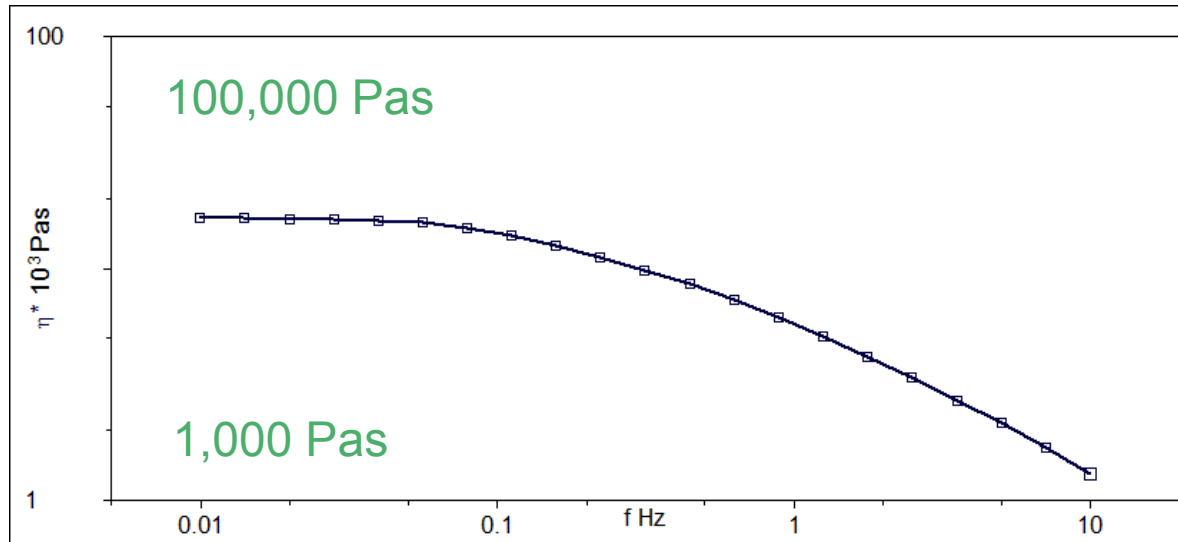
# Kinetic Sand



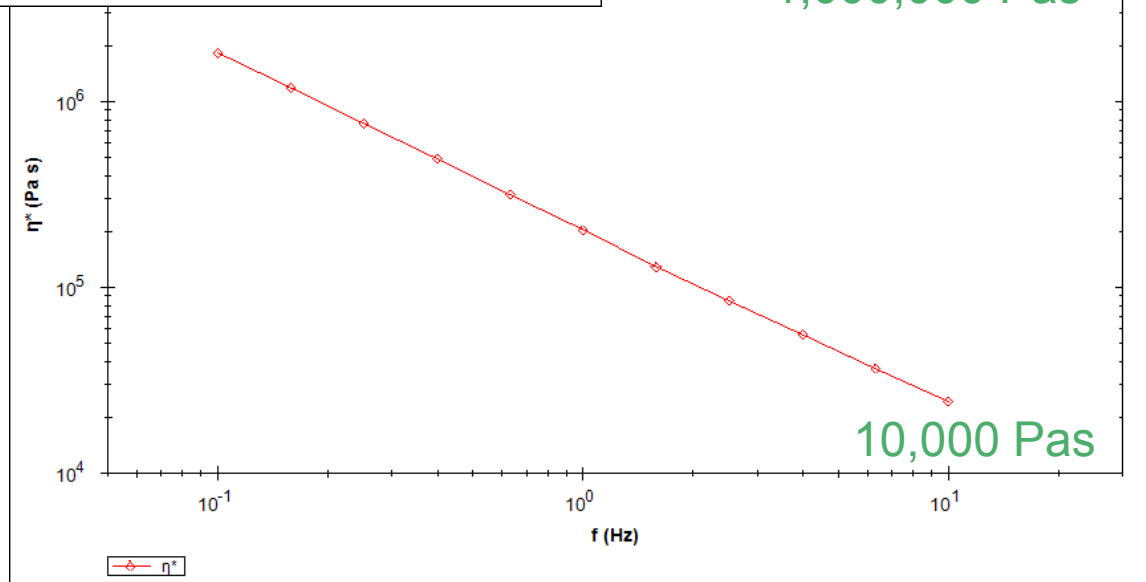




# Kinetic Sand vs. Play Putty

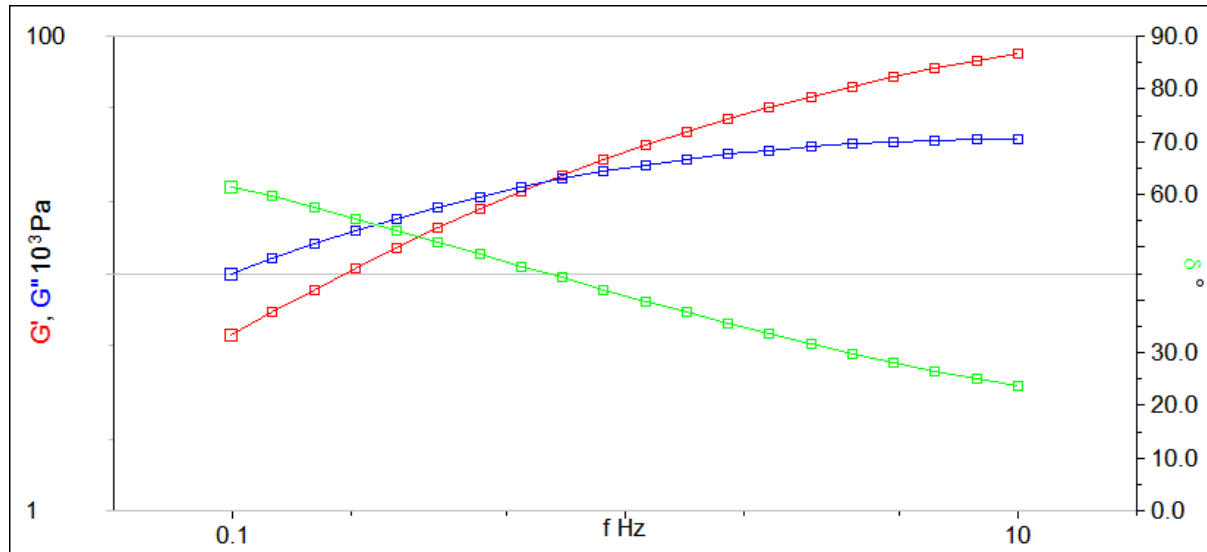


Kinetic Sand





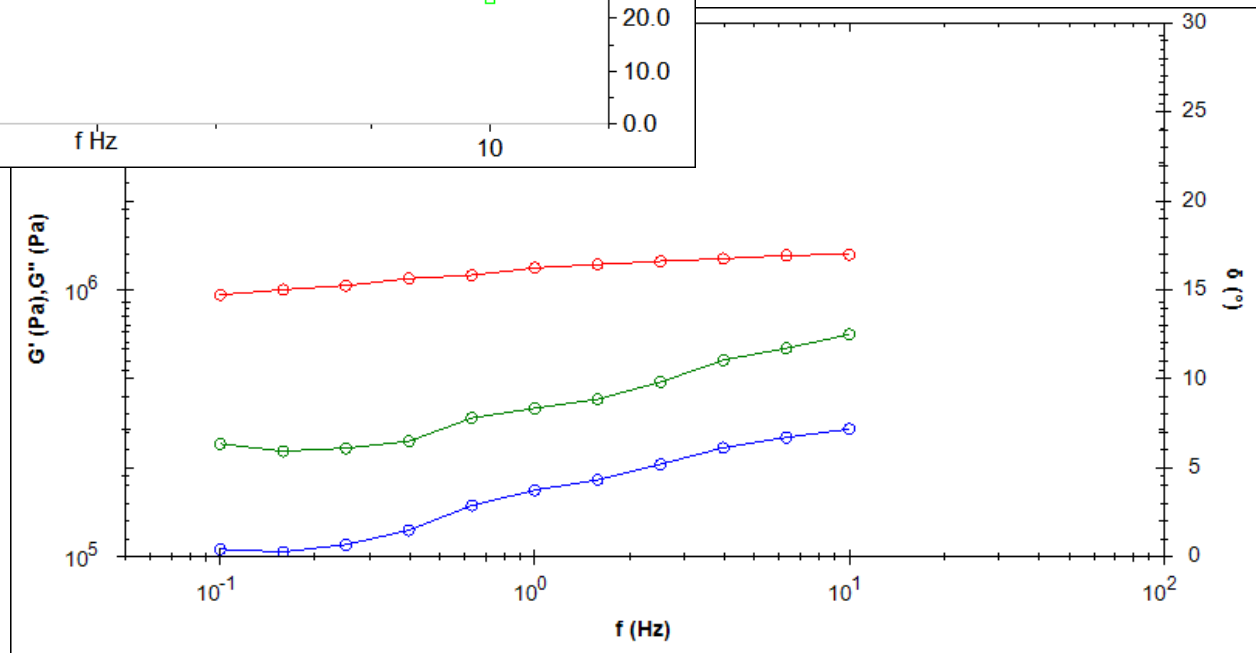
# Kinetic Sand vs Play Putty



## Play Putty

Viscoelastic LIQUID  
Phase angle approaches  
 $90^\circ$  towards 0Hz

Viscoelastic SOLID  
Phase angle approaches  
 $0^\circ$  towards 0Hz  
**Kinetic Sand**



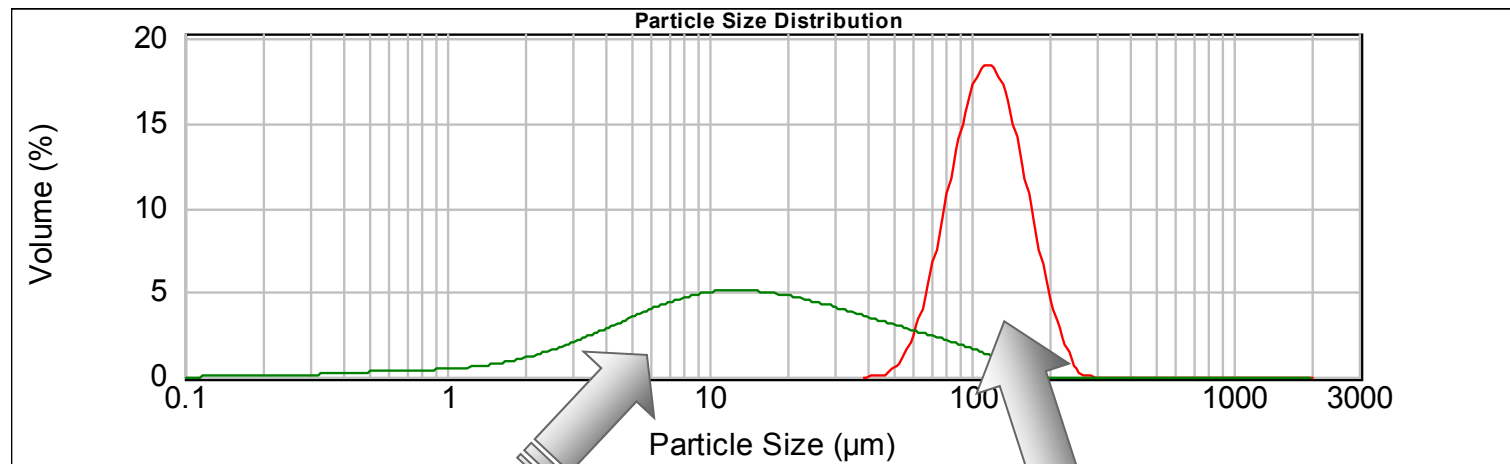


# PARTICLE SIZE DISTRIBUTION

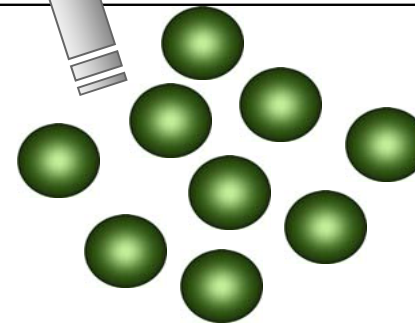
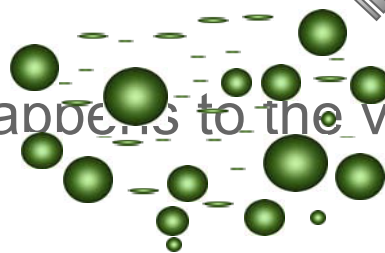


# Effect of particle size distributions

- We can keep the volume fraction ( $\phi$ ) the same.
- Now, change the particle size distribution...



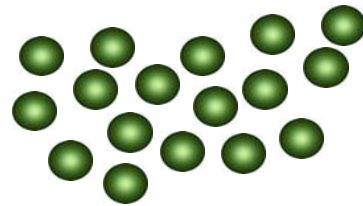
- What happens to the viscosity?



# Effect of Distribution on Maximum Packing Fraction

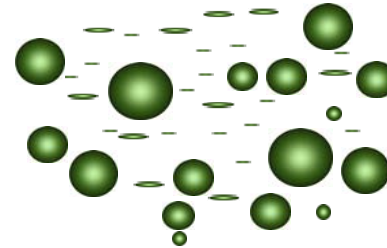
- As the particle size distribution increases, this allows a greater packing fraction.

Random  
monodispersed  
close packing



$$\phi_m \approx 0.62$$

Random  
polydisperse close  
packing



$$\phi_m \geq 0.74$$

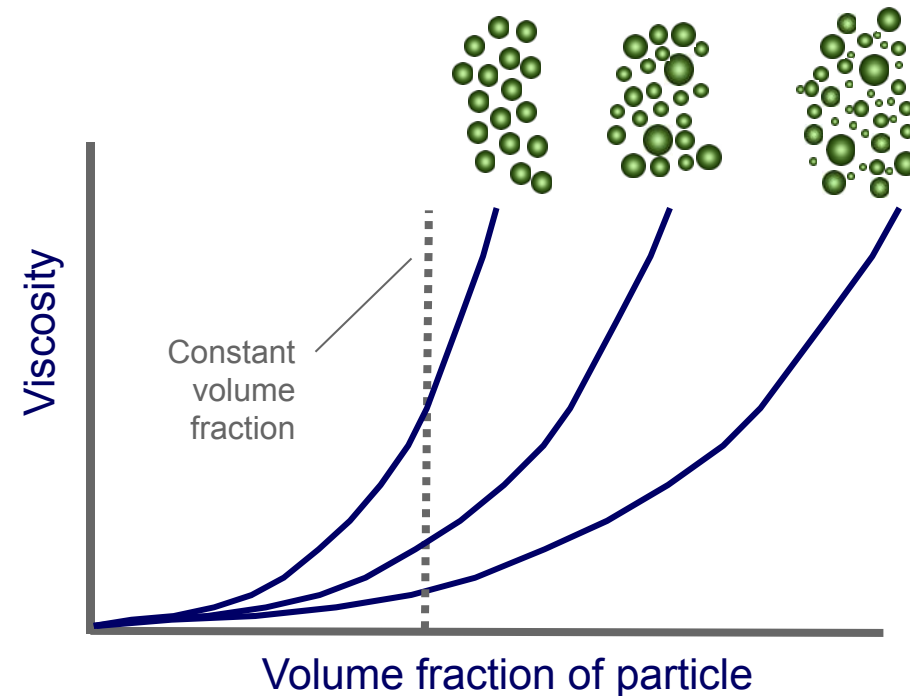


# Effect of Maximum Packing Fraction

- As **maximum packing fraction increases**...



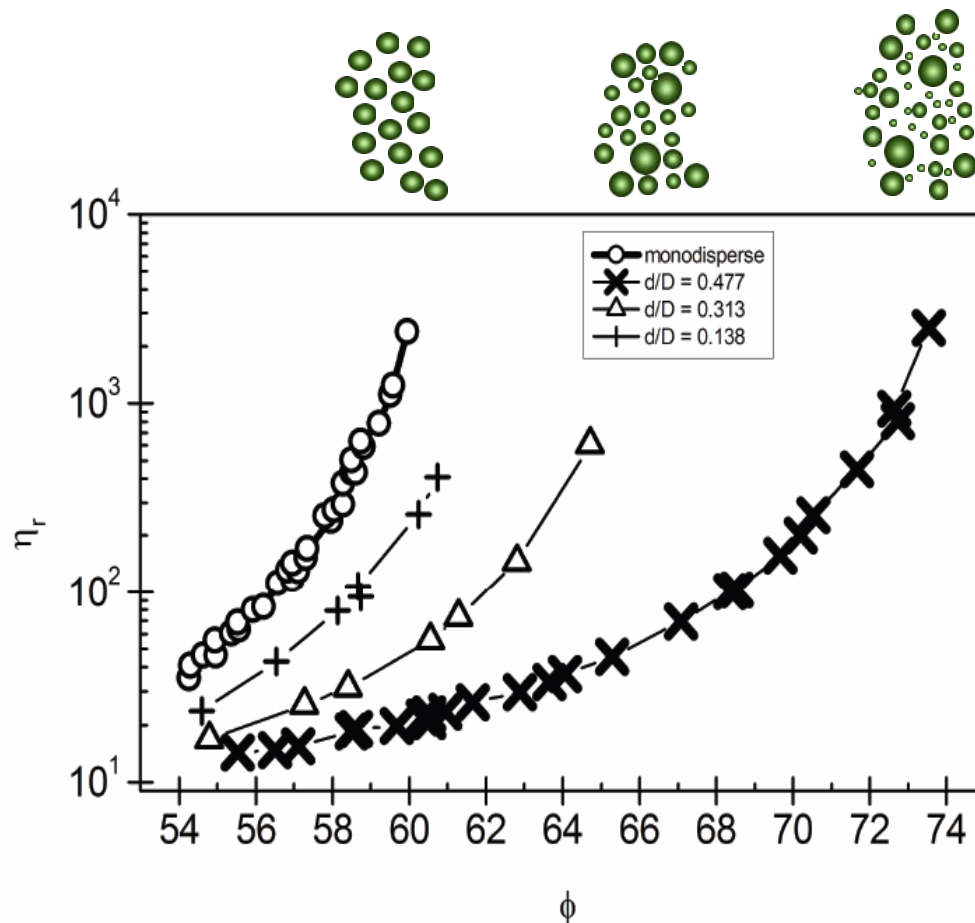
$$\frac{\eta}{\eta_{medium}} = \left(1 - \frac{\phi}{\phi_m}\right)^{-[\eta]\phi_m}$$



- › Then **viscosity ( $\eta$ ) decreases.**
- › Allows more free flowing particles (self lubricating)

# Effect of particle size distribution

- For the same volume fraction and particle size, a **narrow particle size distribution** has a **higher viscosity** compared to a broad particle size distribution.
- As size **distribution increases**,  $\Phi_m$  increases in the Krieger Dougherty equation, resulting in a **reduced viscosity**.



Chong et al. 1971

analytical 2019



Stability



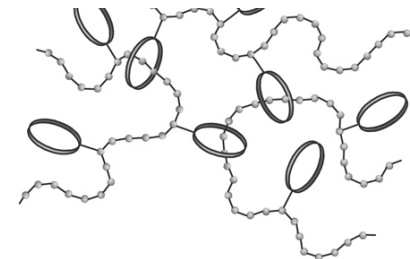
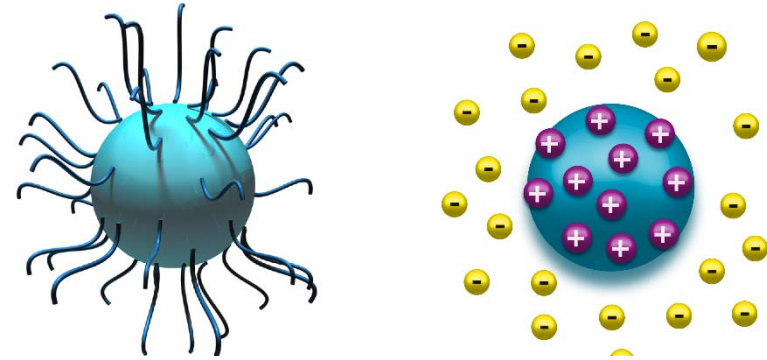
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# How to Achieve Stability?



- Prevent coagulation through **inter-particle repulsion**
- Slow down sedimentation by **increasing viscosity** of continuous phase
- Make it 'solid' by creating a **network structure**



# Stability: Which Method?

.... It Depends



- **Particle radius** ( $a$ ) will have a large bearing on suspension stability
- For **sub micron** particles **Brownian motion** is usually significant to overcome effect of gravity
- For **larger particles** **gravity dominates** if there is a significant density difference ( $\Delta\rho$ )



The Structure and Rheology of Complex Fluids; R Larson

# EXPERIMENTAL EXAMPLE



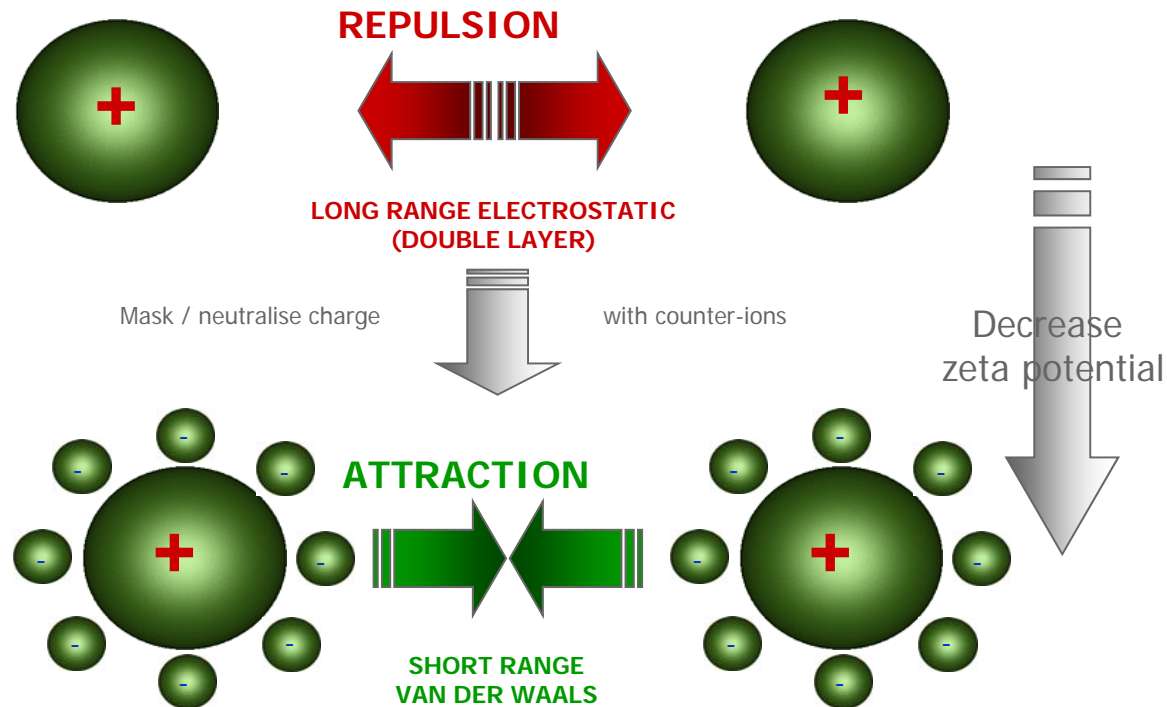
# Experimental

- 75% w/w Silica dispersion made up in deionised water
- Zeta potential evaluated using a Malvern **Zetasizer Nano** ZS with autotitrator
- Particle size evaluated using a Malvern **Mastersizer**
- Rheological properties measured using a **Kinexus** rheometer



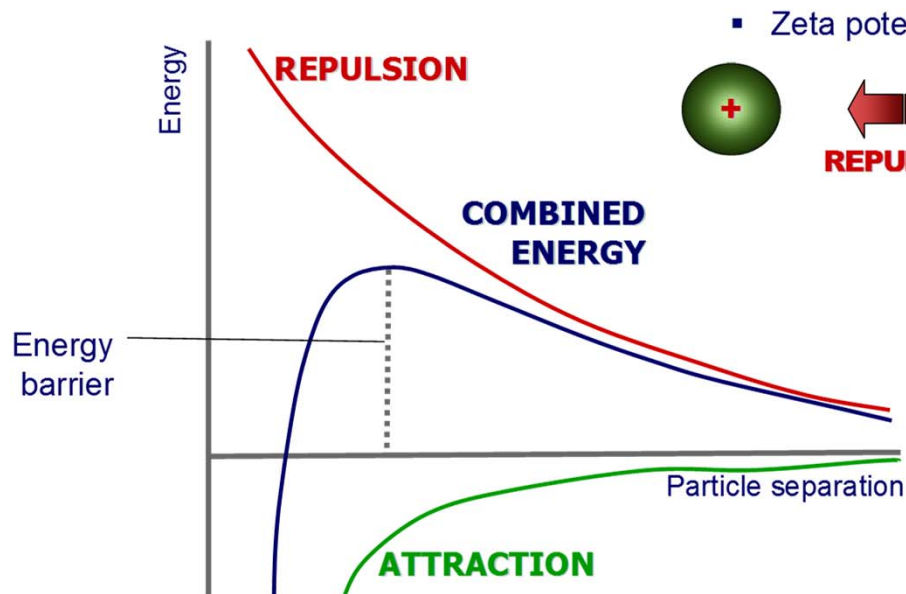
# Colloidal Stability

- To maintain stability through Brownian motion we need to prevent particles sticking when they collide
- This can be achieved by increasing the charge associated with the particle i.e. **zeta potential**.



# Colloidal stability and DLVO Theory

- › An energy barrier resulting from combination of the attractive and repulsive forces prevents particles approaching each other closely.



▪ Zeta potential →  $\pm 30\text{mV}$

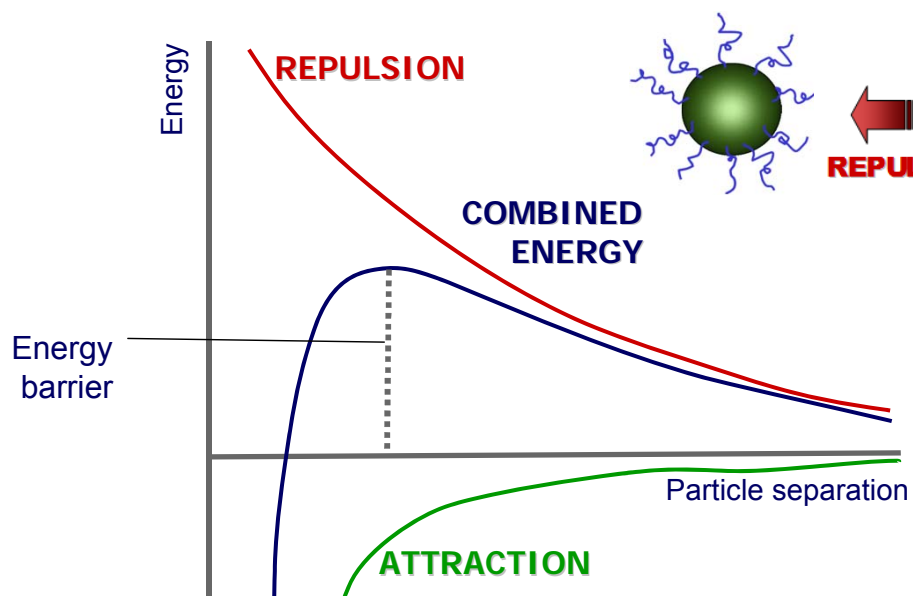


$\pm 30\text{mV}$  considered  
suitable threshold value for  
stability

- › So long as particle Kinetic Energy does not exceed this barrier coagulation should not occur.

# Colloidal stability by steric means

- › An energy barrier can also result by adsorbing of amphiphilic polymers onto the particle surface preventing close approach



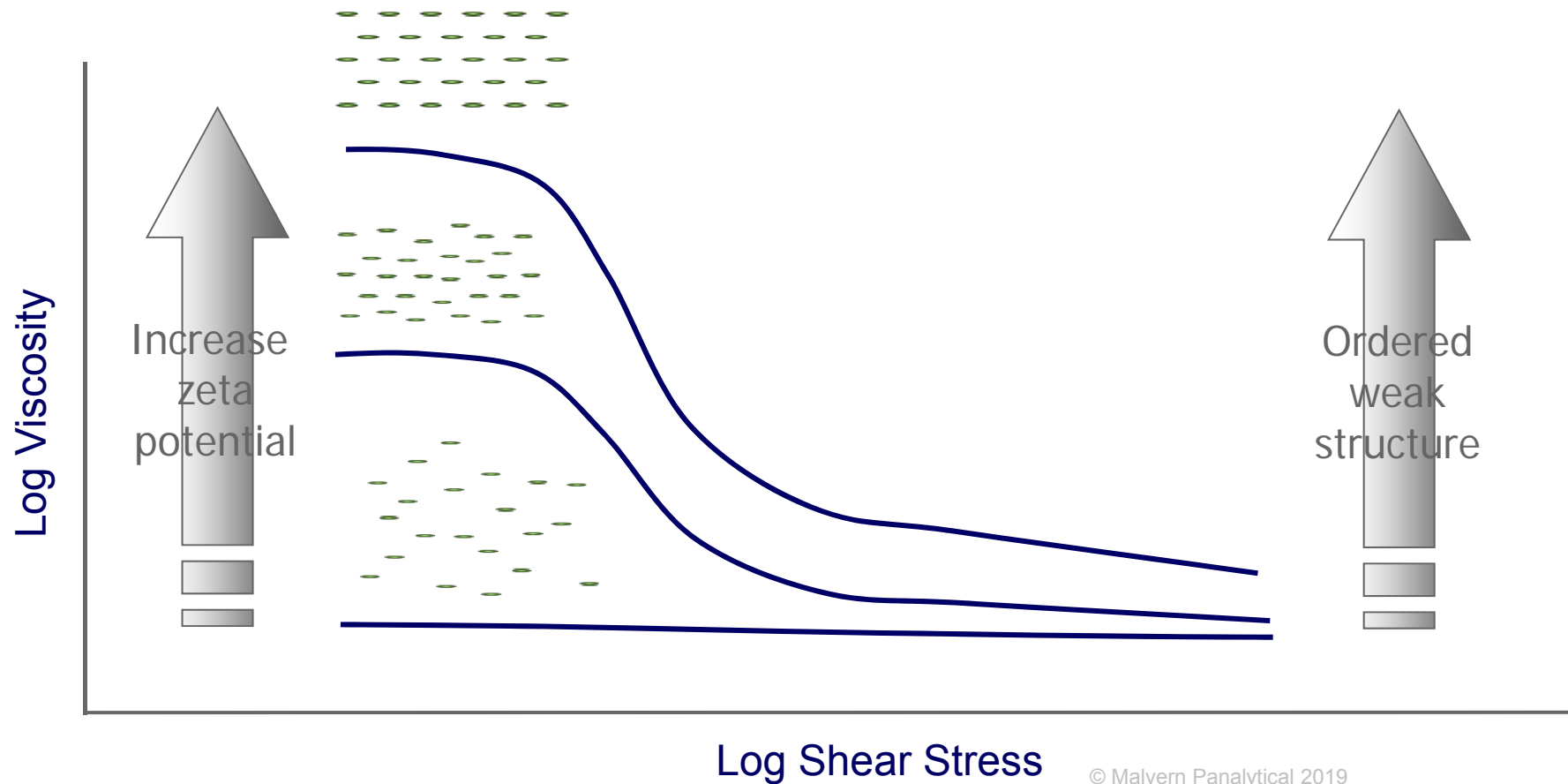
Stability tends to increase with molecular weight, surface coverage and solvent affinity

- › A steric mechanism is likely to be much more efficient in non-aqueous solvents and high electrolyte systems



# Effect of zeta potential on low shear viscosity

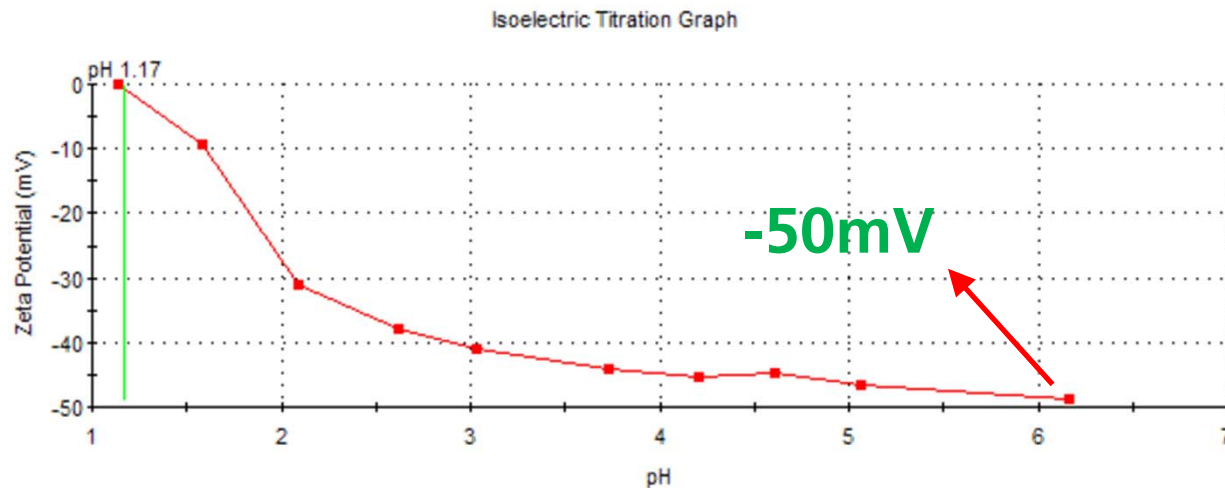
- Low shear viscosity increases with increasing zeta potential thus high charge will help slow down sedimentation



# Silica Dispersion Stability

## Why is it not stable?

- Initial sample evaluation made using at natural pH of dispersion 6.2.
- Despite having a zeta potential of  $-50$  mV the suspension was found to be unstable.



- Lets check particle size...



### Experimental

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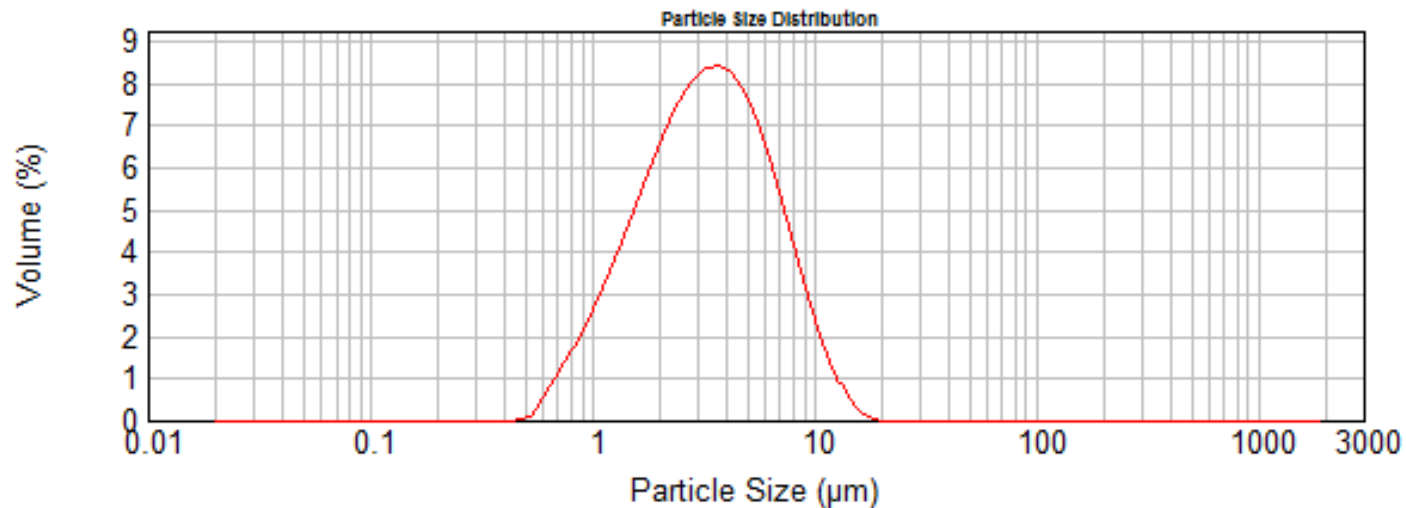


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# Particle Size and Density

- Sample was characterised on a Mastersizer and was found to have a **median particle size of 3.7  $\mu\text{m}$** .
- The **largest** particle was approximately **20  $\mu\text{m}$** .



- Particle density was 2600  $\text{kg}/\text{m}^3$

## Experimental

- › 75% w/w Silica dispersion made up in deionised water.
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# Force Balance on Particle

## Experimental

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- The above relationship for the median particle size (3.7  $\mu\text{m}$ ) gives a value of **45** and for the largest particle (20  $\mu\text{m}$ ) a much higher value of **38,000!!**
- This means that **gravitational forces are dominant** for this sample
- This would explain why **sedimentation occurs** and indicates that another approach is required to induce stability



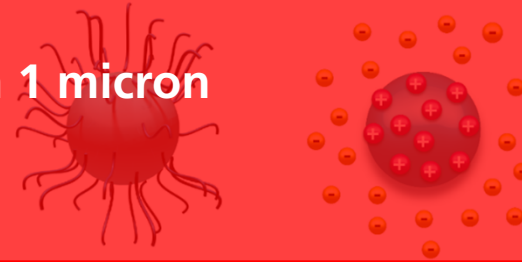
# How to Achieve Stability?

**No one method**

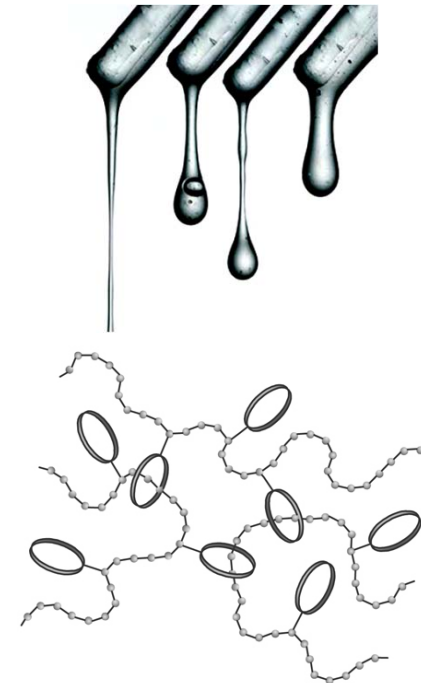


- Prevent coagulation through inter-particle repulsion

**Only for particles less than 1 micron**



- Slow down sedimentation by increasing viscosity of continuous phase
- Make it Solid by creating a network structure





# VISCOSITY / KINETIC STABILITY



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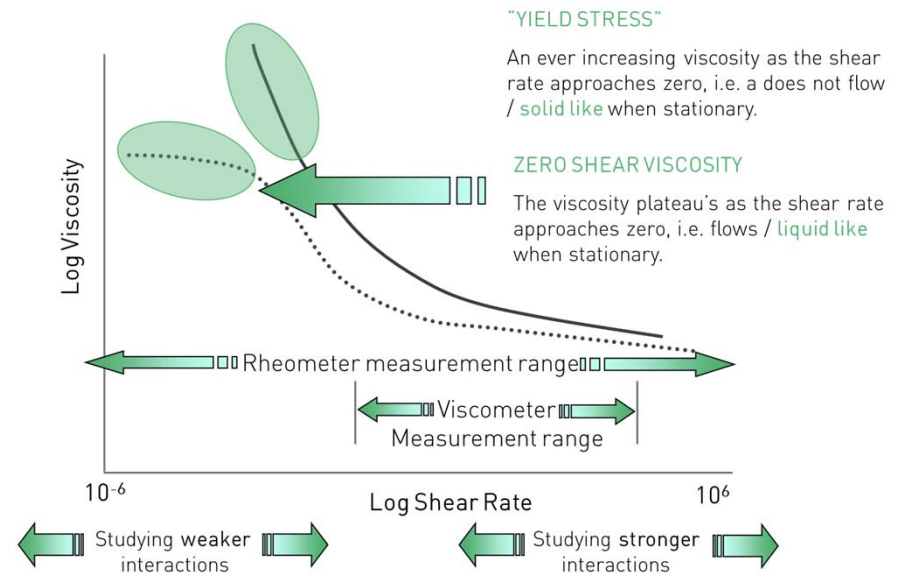
# Effect of Viscosity (Dilute Systems)



- Stokes equation can be used to predict settling velocity ( $V$ ) of a dilute suspension within a continuous phase; viscosity ( $\eta$ )

$$V = \frac{2\Delta\rho g a^2}{9\eta}$$

- Velocity increases with **the square of particle size** making this the most critical parameter
- To slow down sedimentation rate:
  - Increase low shear viscosity
  - Decrease particle size
  - Match density of dispersed and continuous phases



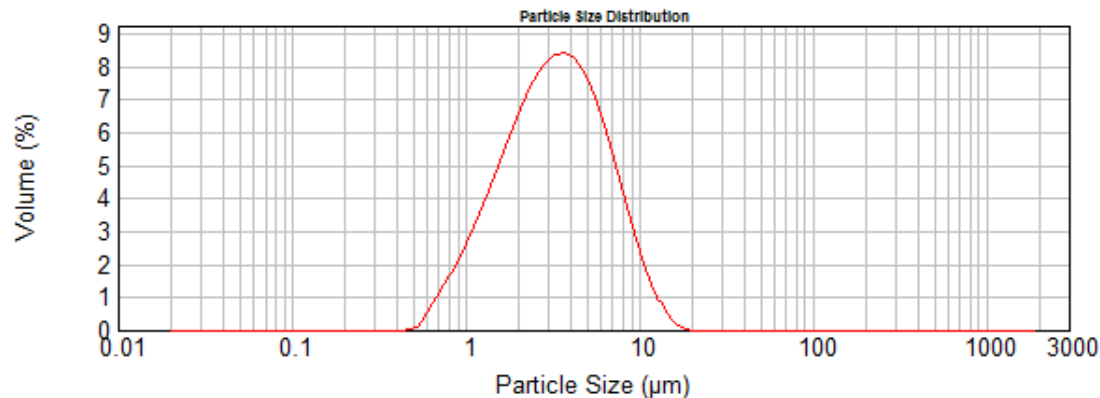


# Silica dispersion, what viscosity?

## Using our example in the equation

- **If 5mm sedimentation per year** was acceptable we would need a viscosity in the region of **11 Pas** for this Silica dispersion

- This is ~11,000 times the viscosity of water! But at low shear...
- Details of a concentrated system modification in the reference below



$$V = \frac{2\Delta\rho g a^2}{9\eta}$$

Barnes, H A (1992), *Recent advances in rheology and processing of colloidal systems*, The 1992 IChemE Research Event, pp. 24-29, IChemE, Rugby

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### Experimental

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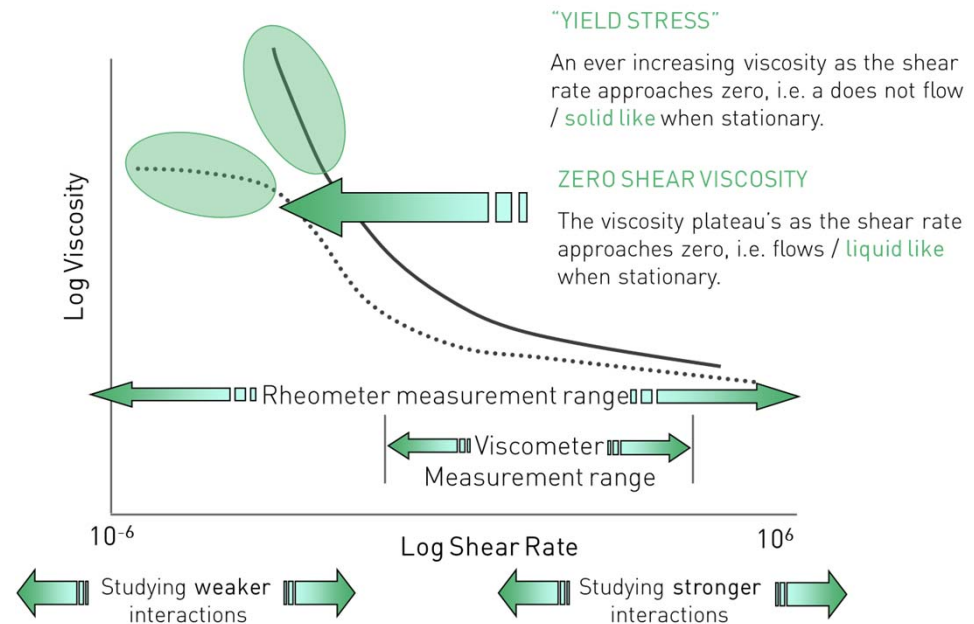
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# Additives for Increasing Low Shear Viscosity



- Alginates
- Methylcellulose
- Acacia gum
- Gellan gum
- Hydroxyethylcellulose
- Bentonite clay
- Laponite clay
- Tragacanth
- Xanthan gum
- Associative Polymers
- Surfactant Lamellar



Choice of thickener will depend on system compatibility and required flow properties – some may induce a yield stress

# Non-colloidal gold!



## Approx. "Particle Size"

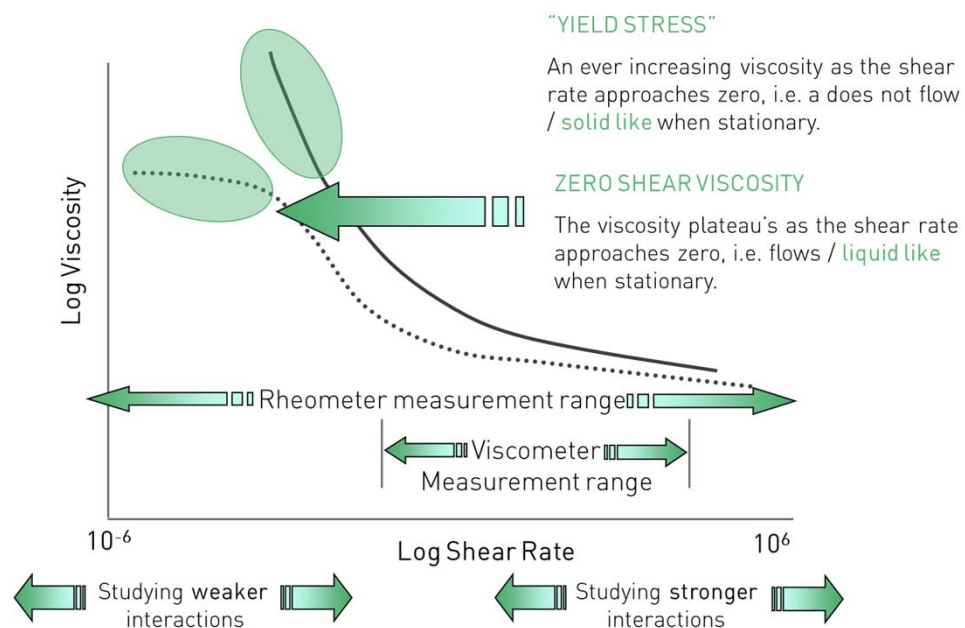
Length 2 mm

Width 2 mm

Thickness 0.1  $\mu$ m

Approx. radius equivalent (a) 45.7  $\mu$ m

# Additives for Increasing Low Shear Viscosity



- Alginates
- Methylcellulose
- Acacia gum
- Gellan gum
- Hydroxyethylcellulose
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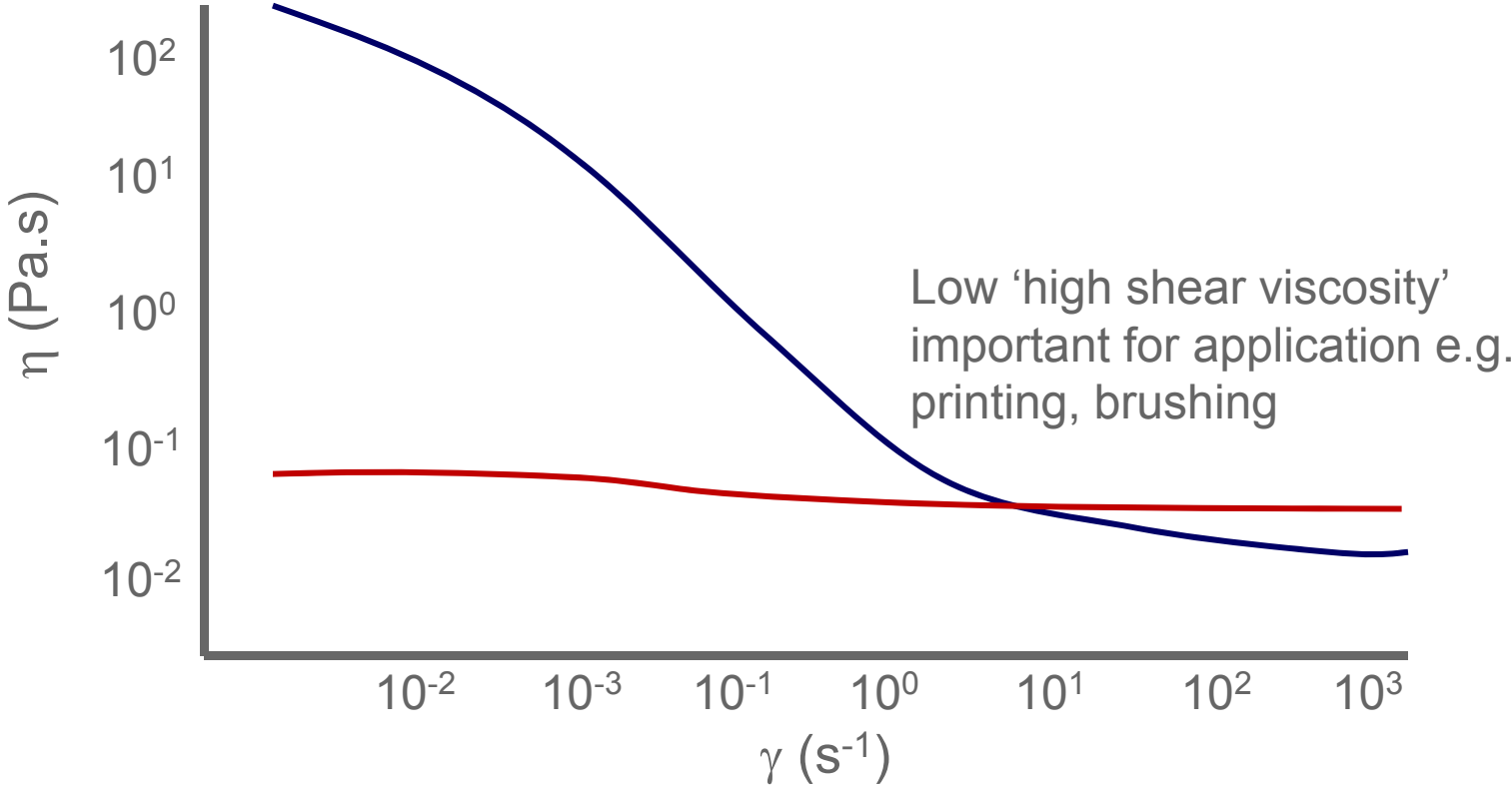




# Maintaining performance and functionality



High 'low shear viscosity' helps to slow down sedimentation



# How to Achieve Stability?

No one method

- Prevent coagulation through inter-particle repulsion

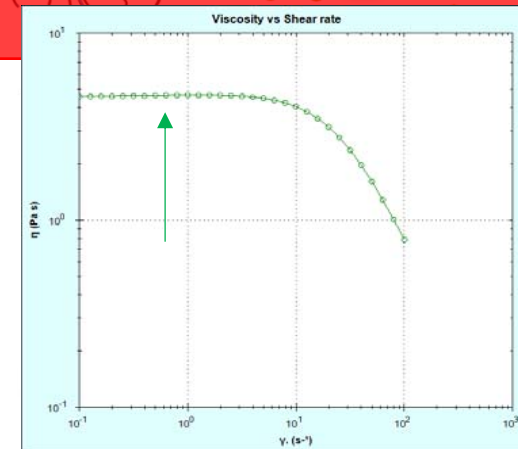
Only for particles less than 1 micron



- Slow down sedimentation by increasing viscosity of continuous phase

**KINETIC STABILITY**

- Make it Solid by creating a network structure





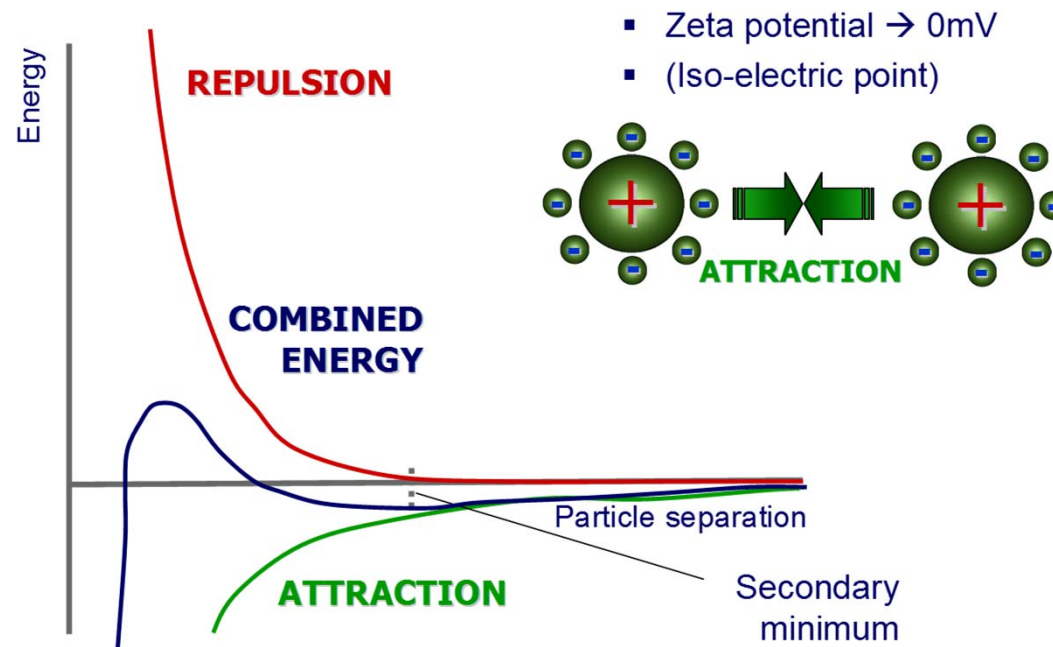
# YIELD STRESS / THERMODYNAMIC STABILITY



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# Colloidal stability and DLVO theory

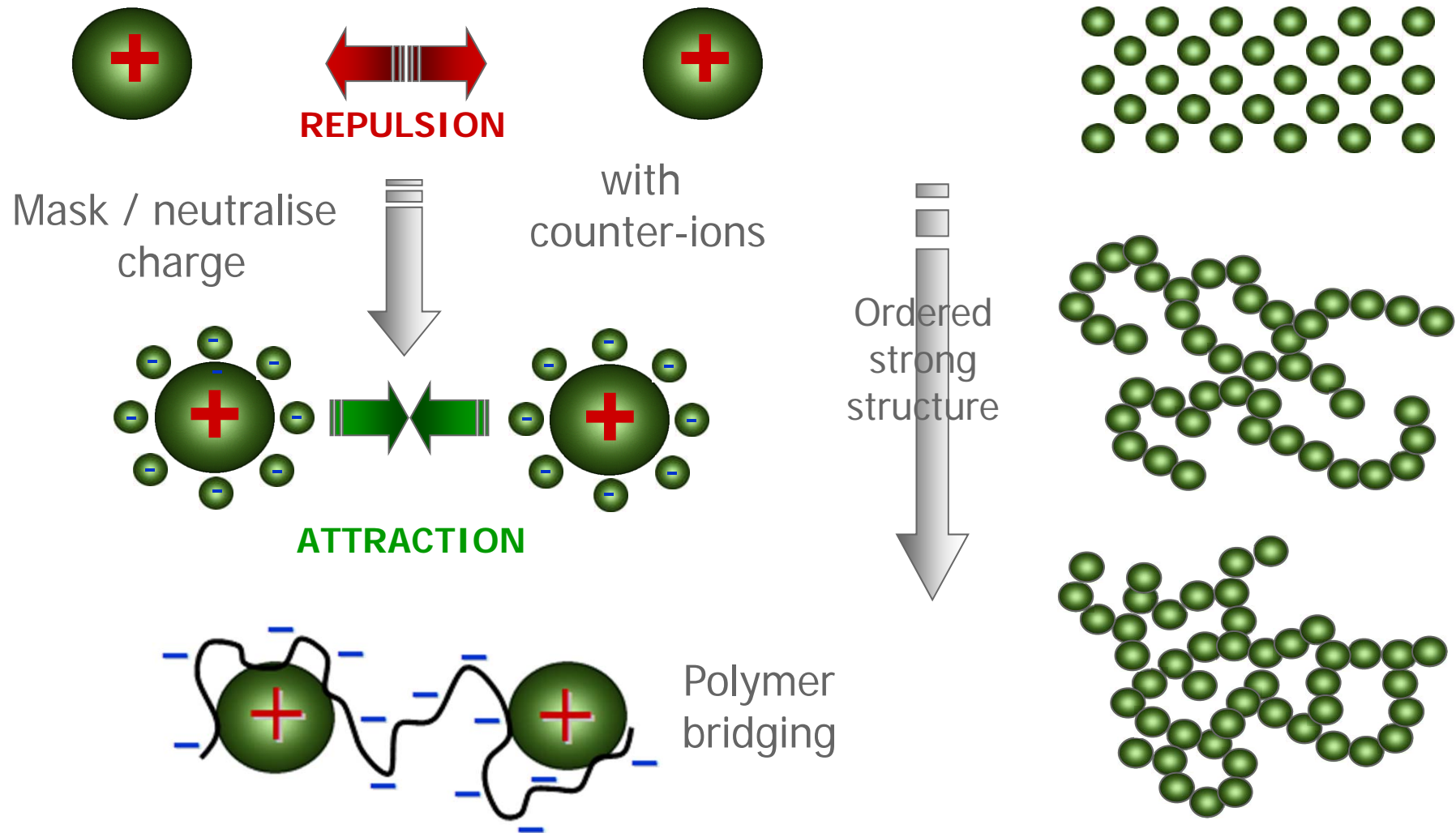
- When electrostatic forces can be minimized it is possible to produce a secondary minimum.



- If secondary minimum is deep enough a strong reversible flocculated network can be formed



# Forces in a stable dispersion



# Zeta Potential

## Experimental

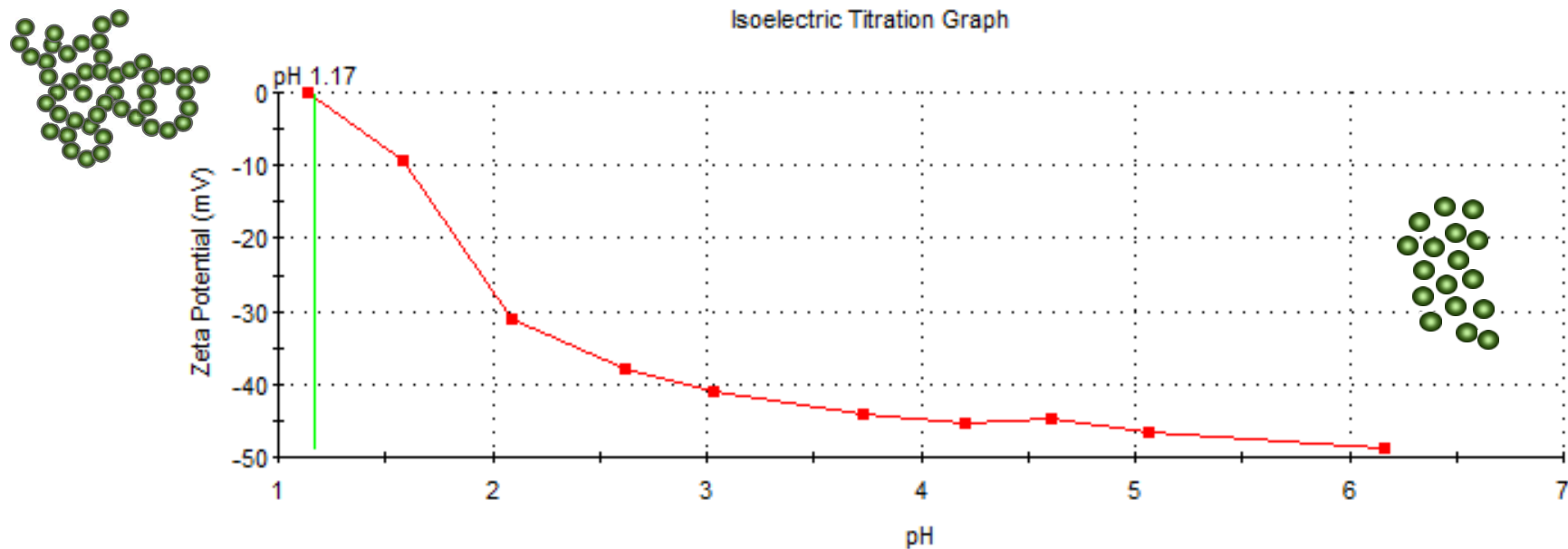
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- Titrating the silica sample with HCl on a Zetasizer Nano with MPT-2 autotitrator.



- The isoelectric point (where the zeta potential is zero) is in the very acidic (pH 1) region.

# Rheology of dispersions at different pH

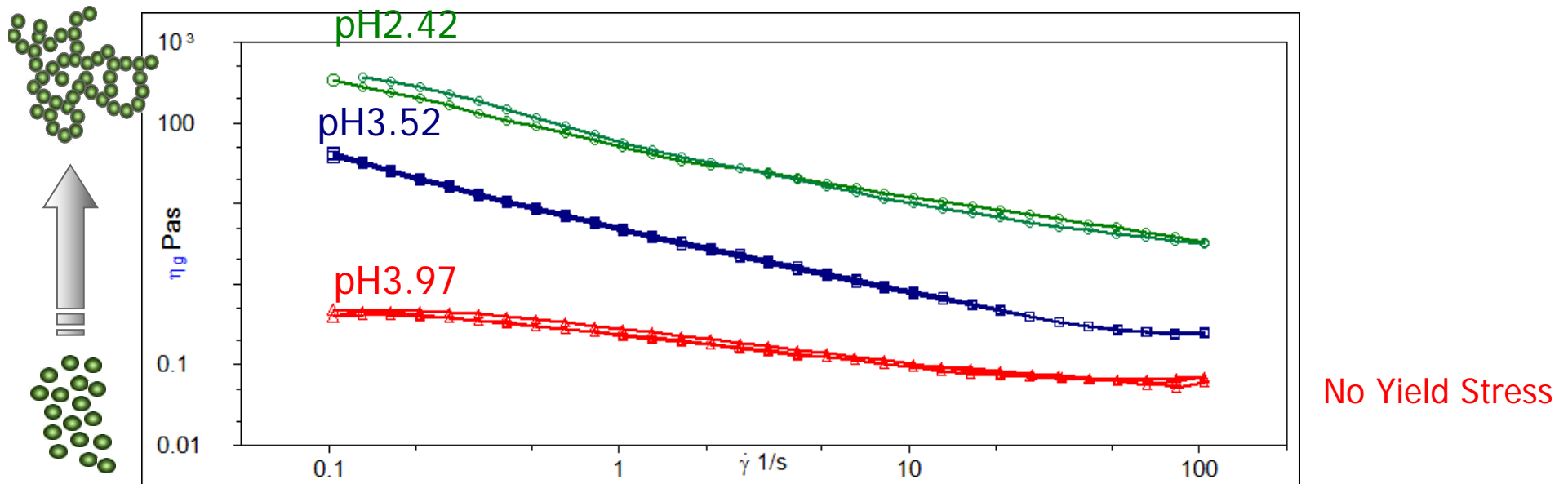
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- At lower pH's particles **associate** more causing an **increase in viscosity** as approaching isoelectric point
- This is favourable for stability

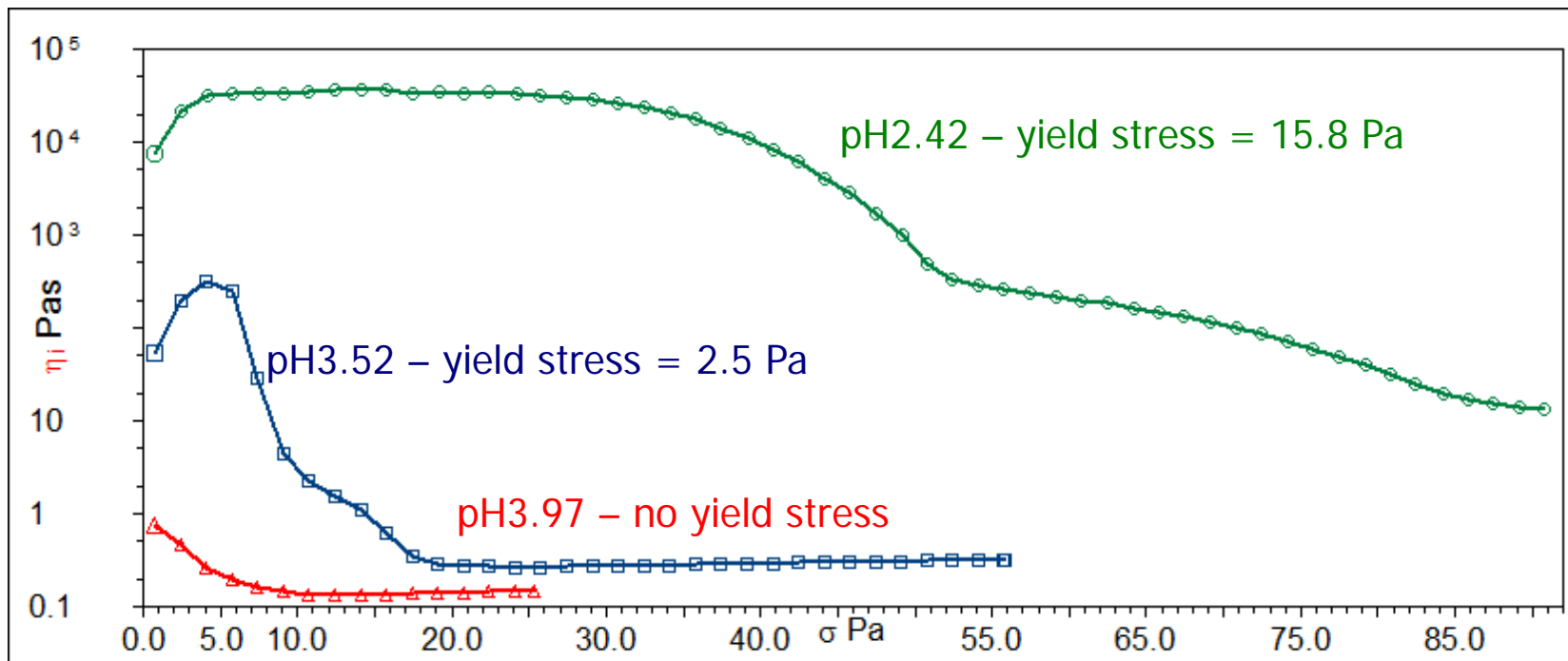


No Yield Stress

- Low pH samples show no viscosity plateau suggesting solid like behaviour at rest
- Measurements repeated on the same loaded sample indicate reversible flocculation due to a secondary minimum

# Yield Stress

- At high pH there is no elastic network hence no yield stress observed.
- As pH is lowered stronger interactions occur leading to larger yield stress.



# What Yield Stress is sufficient?

- For a particle to stay suspended the **yield stress must exceed the gravitational force** acting on the particle
- This can be estimated from the following equation:

$$\sigma_y = Y(\rho_D - \rho_C)rg$$

- Y is the **critical yield parameter** (0.33 for Stokes law) which has been shown to have a range of values based on various studies
- For the **silica** sample, a  **$\sigma_y$  of just 0.1 Pa** will do!

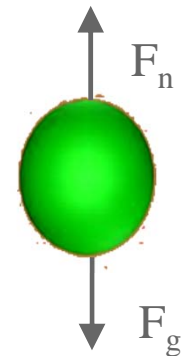
*P. B. Laxton and J. C. Berg. Gel trapping of dense colloids. J. Colloid Interface Sci. 285:152–157 (2005)*

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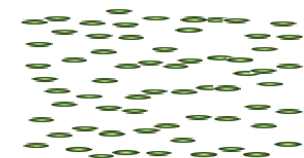
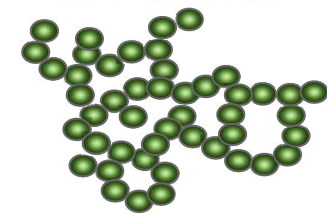
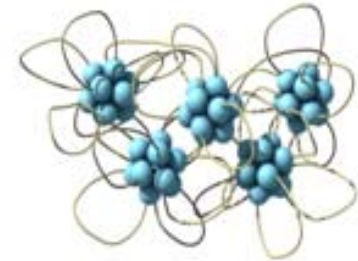
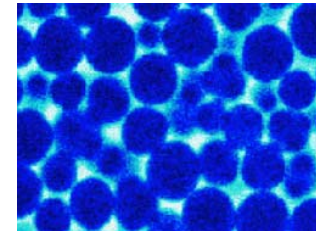
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# Yield Stresses Occur In.....



- **Emulsions, foams and dispersions** where components are tightly **packed** together
- **Associative polymers** that interact strongly enough to form an **extended network** through the dispersion medium
- **Flocculated dispersions** which form a strong **extended network**
- **Glassy materials** which are essentially **frozen in** a solid state



# How to Achieve Stability?

No one method

- Prevent coagulation through inter-particle repulsion
- Only for particles less than 1 micron

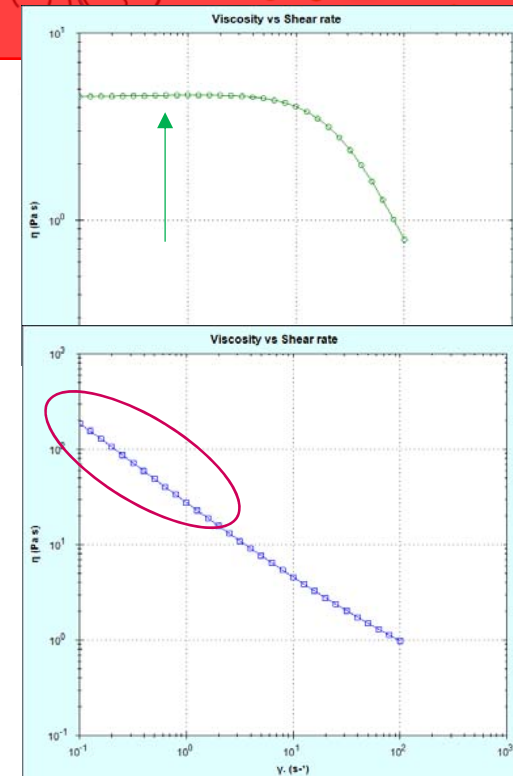


- Slow down sedimentation by increasing viscosity of continuous phase

**KINETIC STABILITY**

- Make it Solid by creating a network structure

**THERMODYNAMIC STABILITY**



# Summary - Stable suspensions



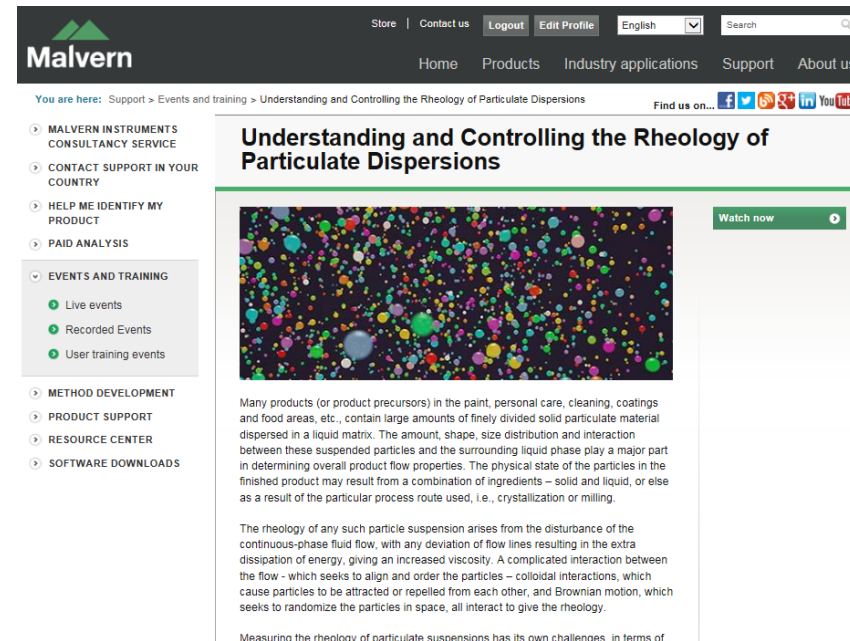
- Particle sizes  $< 1 \mu\text{m}$ 
  - Create a large **charge on the particle**,  $\pm 30 \text{ mV}$
  - Optimise for long range electrostatic repulsion
  - More stable with higher LOW shear viscosity
- Particle sizes  $> 1 \mu\text{m}$  (depending on density)
  - Now particles are large enough that gravity has an effect
  - **Rheology** is now needed to make a stable dispersion
  - Induce a **yield stress** through network forming polymers or clays
  - Slow down sedimentation by **increasing low shear viscosity** through use of appropriate additives



# Useful Links



- <http://accessintelligence.imirus.com/Mpowered/book/vchei15/i1/p1>
  - Search: “chemengonline paint a clear picture”
- <http://www.malvern.com/en/support/events-and-training/webinars/W160922RheologyParticulateDispersions.aspx>
  - Search: “malvern understanding controlling rheology particulate”



The background is a solid teal color with a pattern of diagonal stripes in a lighter shade of teal, creating a textured effect.

Thank you for your attention

Any Questions?

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